

**UNCLASSIFIED**

**AD \_ 408 402 \_**

**DEFENSE DOCUMENTATION CENTER**

**FOR**

**SCIENTIFIC AND TECHNICAL INFORMATION**

**CAMERON STATION, ALEXANDRIA, VIRGINIA**



**UNCLASSIFIED**

NOTICE: When government or other drawings, specifications or other data are used for any purpose other than in connection with a definitely related government procurement operation, the U. S. Government thereby incurs no responsibility, nor any obligation whatsoever; and the fact that the Government may have formulated, furnished, or in any way supplied the said drawings, specifications, or other data is not to be regarded by implication or otherwise as in any manner licensing the holder or any other person or corporation, or conveying any rights or permission to manufacture, use or sell any patented invention that may in any way be related thereto.

63 4-2

CATALOGED BY DDC  
AS AD No. 408402

408 402

**BRL**

REPORT NO. 1202  
APRIL 1963

**PARTIALLY CONSTRAINED IMPINGING JETS**

J. H. Giese

JUL 12 1963  
LIBRARY A

RDT & E Project No. 1M010501A003  
**BALLISTIC RESEARCH LABORATORIES**

**ABERDEEN PROVING GROUND, MARYLAND**

**ASTIA AVAILABILITY NOTICE**

Qualified requestors may obtain copies of this report from ASTIA.

The findings in this report are not to be construed  
as an official Department of the Army position.

BALLISTIC RESEARCH LABORATORIES

REPORT NO. 1202

APRIL 1963

PARTIALLY CONSTRAINED IMPINGING JETS

J. H. Giese

Computing Laboratory

RD&E Project No. 1M010501A003

ABERDEEN PROVING GROUND, MARYLAND

BALLISTIC RESEARCH LABORATORIES

REPORT NO. 1202

JHGiese/mec  
Aberdeen Proving Ground, Md.  
April 1963

PARTIALLY CONSTRAINED IMPINGING JETS

ABSTRACT

Qualitative explanations of the motion of shaped charge liners have been based on impact of two plane jets in which the moving fluid is surrounded by four stagnant regions, all at the same pressure. Actually, the motion is initiated by the difference between the high pressure in the detonation products on one side of the liner and atmospheric pressure on the other. This report considers symmetrical impact of two jets, each partially constrained on one or both sides, in which the stagnant regions are not all at the same pressure.

# TABLE OF CONTENTS

	Page
ABSTRACT . . . . .	3
1. INTRODUCTION . . . . .	7
2. MATHEMATICAL FORMULATION OF PROBLEM . . . . .	8
3. CONFORMAL MAPPING OF HODOGRAPH IMAGE ONTO HALF-PLANE . . . . .	9
4. CONSTRUCTION OF $f(w)$ . . . . .	11
5. PARTIALLY CHANNELLED IMPINGING JETS . . . . .	14

## 1. INTRODUCTION

Treatises on hydrodynamics generally contain discussions of two standard examples of plane incompressible jet flows; viz.:

a. Efflux of liquid with high pressure at infinity from a reservoir with straight walls into a jet surrounded by stagnant fluid at lower pressure;

b. Impact of two jets, in which the moving fluid is surrounded by four regions of stagnant fluid, all at the same pressure.

Contemplation of these examples suggests the problem, to determine the following flow:

c. Impact of two jets, each partially constrained on one side by straight walls, in which the jets are also partially bounded by four regions of stagnant fluid, not all at the same pressure.

The symmetrical form of (c), shown schematically in Fig. 1 (with an inflection point  $A_4$  on the high pressure boundary), will be discussed in this note.

A perfectly obvious generalization of (c) is

d. Impact of two jets, each partially constrained on both sides by straight walls, in which the jets are also bounded by four regions of stagnant fluid, not all at the same pressure.

The symmetrical form of this flow is discussed at the end of this note by straight forward modifications of the mathematical apparatus used to describe (c).

The flows to be constructed are interesting for their own sakes as jets that can be described explicitly in relatively simple terms. Additional interest might be stimulated by the following considerations. Flows of type (b) have been used to suggest a qualitative explanation of the motion of the liner of a shaped charge. In reality, the motion is produced by the difference between the high pressure in the detonation products on one side of the liner and atmospheric pressure on the other side. Furthermore, at an intermediate stage only part of the liner has collapsed or begun to collapse, while the rest is still rigid. In an admittedly imperfect way flows (c) and (d) more nearly approximate these features than (b).

We note also that various pressures, velocities, and widths are referred to in Fig. 1, and four additional parameters will appear in the discussion in the following sections. Let us suppose we have experimental measurements of the angles  $\theta_3, \theta_4$ , the three widths  $h_1, h_3$ , and  $h_5$ , and assume we know  $p_1$  (which might be atmospheric pressure) and the density  $\rho$  of the jets. Then we could apply the seven equations (2.3), (3.4) - (3.6), (4.4), (4.6), and (4.8) to determine the four relatively uninteresting mathematical parameters and the three important physical parameters  $p_5, U_1$ , and  $U_5$ , (which will be defined in equations 2.4 and 2.5).

## 2. MATHEMATICAL FORMULATION OF PROBLEM

Plane irrotational incompressible flow can be characterized by a complex potential function

$$(2.1) \quad \Phi(z) = \phi + i\psi.$$

Here  $\Phi(z)$  is an analytic function of the complex variable  $z = x + iy$ ,  $\phi$  is the velocity potential function,  $\psi$  the stream function, and

$$(2.2) \quad w = u - iv = d\Phi/dz$$

is the complex velocity. The pressure  $p$  within the jets is determined by Bernoulli's equation

$$(2.3) \quad p + \frac{1}{2} \rho |w|^2 = \text{constant}$$

Conditions on the jet boundaries are characterized by

$$(2.4) \quad p = p_\alpha, \quad \alpha = 1, 5,$$

and thus  $|w|$  assumes corresponding constant values

$$(2.5) \quad |w| = U_\alpha, \quad \alpha = 1, 5.$$

To seek  $\Phi(z)$  or  $w(z)$  directly in the  $z$ -plane is hopeless, since the location of the jet boundaries characterized by (2.4) or (2.5) is not known a priori. The classical artifice for overcoming this difficulty is to invert (2.2) to determine

$$(2.6) \quad z = f(w)$$

where  $f$  is an analytic function of  $w$ . Then straight-streamlines (walls, or the axis of symmetry) have as their images in the  $w$  - or hodograph-plane segments of lines through the origin, and free jet boundaries correspond to arcs

of circles (2.5) with centers at the origin. Thus the impinging jets of Fig. 1 map onto the interior of the region shown in Fig. 2. The circular cuts  $A_3A_4$  and  $A_2A_4$  appear as a matter of necessity, while the cut  $A_5A_6$  has been introduced for later convenience.

Boundary conditions and other relevant properties of  $f(w)$  can be determined as follows. On the straight streamlines of Fig. 1  $dz$  is parallel to  $\bar{w}$  and  $dw$  is parallel to  $w$ . Thus on all straight segments shown in Fig. 2

$$(2.7) \quad \operatorname{Im} w^2 dz/dw = \operatorname{Im} w^2 f'(w) = 0$$

On the free jet boundaries, which are also streamlines,  $dz$  is again parallel to  $\bar{w}$ , and on the circular arcs (2.5)  $dw$  is parallel to  $iw$ . Thus on all circular arcs shown in Fig. 2

$$(2.8) \quad \operatorname{Re} w^2 dw/dz = \operatorname{Re} w^2 f'(w) = 0$$

To guarantee finite non-zero jet widths at infinity in the  $z$ -plane,  $f(w)$  should have logarithmic singularities at  $A_1, A_3, A_3', A_5$ . At  $A_2, A_2', A_4, A_4'$  and at  $A_6$  the function  $f(w)$  should be finite, and as a matter of convenience, arbitrarily choose

$$(2.9) \quad f(\infty) = 0.$$

### 3. CONFORMAL MAPPING OF HODOGRAPH IMAGE ONTO HALF-PLANE

As an aid to determining the functional form of  $w^2 f'(w)$  it will be convenient to map the interior of the curve shown in Fig. 2, slit along  $A_5A_6$ , onto a half plane. To do this, first note that

$$(3.1) \quad W = \log (w/U_1)$$

maps the region in question onto the region with polygonal boundary shown in Fig. 3. If we take account of symmetry, then by the Schwarz-Christoffel formula,

$$(3.2) \quad W = -\alpha \int_0^\xi \frac{(\xi^2 - a_4^2) d\xi}{[(\xi^2 - 1)(\xi^2 - a_3^2)(\xi^2 - a_5^2)]^{0.5}}$$

where  $1 \leq a_3 \leq a_4 \leq a_5$  will, for suitable choices of the positive parameters  $\alpha$ ,  $a_3$ ,  $a_4$ , and  $a_5$  yield the desired mapping onto the upper half of the  $\xi$ -plane.

In the calculation of (3.2), use that branch of the integrand that is positive for  $\xi > a_5$ . For later reference we also note that

$$(3.3) \quad \frac{1}{w} \frac{dw}{d\xi} = - \frac{\alpha (\xi^2 - a_4^2)}{[(\xi^2 - 1)(\xi^2 - a_3^2)(\xi^2 - a_5^2)]^{0.5}}$$

$$(3.4) \quad \alpha I_1 = \alpha \int_0^1 \frac{(a_4^2 - \xi^2) d\xi}{[(1 - \xi^2)(a_3^2 - \xi^2)(a_5^2 - \xi^2)]^{0.5}} = -\theta_3$$

$$(3.5) \quad \alpha I_2 = \alpha \int_1^{a_3} \frac{(a_4^2 - \xi^2) d\xi}{[(\xi^2 - 1)(a_3^2 - \xi^2)(a_5^2 - \xi^2)]^{0.5}} = \log U_1/U_5$$

$$(3.6) \quad \alpha I_3 = \alpha \int_{a_3}^{a_4} \frac{(\xi^2 - a_4^2) d\xi}{[(\xi^2 - 1)(\xi^2 - a_3^2)(a_5^2 - \xi^2)]^{0.5}} = \theta_3 - \theta_4$$

$$(3.7) \quad \alpha I_4 = \alpha \int_{a_4}^{a_5} \frac{(\xi^2 - a_4^2) d\xi}{[(\xi^2 - 1)(\xi^2 - a_3^2)(a_5^2 - \xi^2)]^{0.5}} = \pi + \theta_4$$

The constant  $\alpha$  can be evaluated as follows. Since the only singularities of  $dW/d\xi$  are at  $\pm 1$ ,  $\pm a_3$ , and  $\pm a_5$ , then

$$-4\alpha i(I_1 + I_3 + I_4) = \int_{C_1 + C_2 + C_3} (dW/d\xi) d\xi = \int_C (dW/d\xi) d\xi$$

where  $C_1$ ,  $C_2$ , and  $C_3$  are paths shown schematically in Fig.4, and  $C$  is a circle  $|\xi| = \text{const} > a_5$ . Clearly

$$\int_C (dW/d\xi) d\xi = -\alpha \int_0^{2\pi} (\xi^{-1} + \dots) d\xi = -2\pi i \alpha$$

Since by (3.4) to (3.7),  $-4\alpha i (I_1 + I_3 + I_4) = -4\pi i$ , this yields

$$(3.8) \quad \alpha = 2.$$

#### 4. CONSTRUCTION OF $f(w)$

Recall that  $w^2 f'(w)$  is alternately real or pure imaginary on the segments of the real axis of the  $\xi$  plane with end points  $A_\gamma$  and  $A'_\gamma$ , for  $\gamma = 2, 3, 5$ . Thus it must have branch points at these places, and should contain a factor

$$(\xi^2 - 1)^{r/2} (\xi^2 - a_3^2)^{s/2} (\xi^2 - a_5^2)^{t/2}$$

where  $r$ ,  $s$ , and  $t$  are odd integers. Since  $f$  should have logarithmic singularities at  $A_1$ ,  $A_8$  and  $A'_8$ ,  $\delta = 3, 5$ , then  $df/d\xi$  should have simple poles at the corresponding points. Since furthermore  $f$  should be finite at  $A_2$  and  $A'_2$  this suggests the form

$$(4.1) \quad w^2 f'(w) = \frac{\beta (\xi^2 - 1)^{0.5}}{\xi (\xi^2 - a_3^2)^{0.5} (\xi^2 - a_4^2) (\xi^2 - a_5^2)^{0.5}}$$

The factor  $\xi^2 - a_4^2$  in the denominator will enable us to include the case  $a_4 = a_3$  in the following discussion. Now, by (4.1) and (3.3)

$$(4.2) \quad \frac{df}{d\xi} = \frac{-2\beta}{w} \frac{1}{\xi (\xi^2 - a_3^2) (\xi^2 - a_5^2)}$$

where  $\beta > 0$  merely determines the geometrical scale in the  $z = f(\xi)$  plane. Since  $w(\infty) = 0$ , then by (2.9)  $f(w(\infty)) = f(0) = 0$ , and

$$(4.3) \quad f(\xi) = \int_{\infty}^{\xi} (df/d\xi) d\xi.$$

The uniqueness of our choice for (4.1) can be shown as follows. Let us multiply the left members of (4.1) and (4.2) by an analytic function  $H(\xi)$ . To preserve the alternation of real and imaginary values of  $w^2 f'(w)$  on the real axis,  $H$  must be real there. To prevent the introduction of new branch points and singularities,  $H$  must have no singularities in the closed upper-half plane, and the analytical continuation of  $H$  into the lower half plane is also free of singularities. Hence  $H$  is constant.

It remains to show that  $f(w)$  has the desired properties at  $A_1, A_6, A_\gamma$ , and  $A'_\gamma$ . First note that  $\xi = 0$  corresponds to  $w = U_1$ . Thus by (3.1) and (3.2)

$$\xi = (w - U_1) g(w - U_1)$$

where  $g$  is an analytic function of  $w - U_1$  and  $g(0) \neq 0$ . Since  $df/d\xi$  has a simple pole at  $\xi = 0$ , then  $f(w(\xi))$  has a logarithmic singularity there, and thus  $f(w)$  also has a logarithmic singularity at  $w = U_1$ . A similar argument determines the behavior of  $f$  at  $\xi = \pm a_3$  or  $\pm a_5$ , with the unimportant difference that, for example, (3.1) and (3.2) imply

$$(\xi - a_3)^{0.5} = (w - U_5 e^{-i\theta_3}) h(w - U_5 e^{-i\theta_3})$$

where  $h$  is analytic,  $h(0) \neq 0$ , etc. Hence  $f(w)$  has the required logarithmic singularities.

By (3.2), in the neighborhood of infinity

$$\frac{dW}{d\xi} = -2 \sum_{n=1}^{\infty} c_n \xi^{-n}$$

where  $c_1 = 1$ . Hence  $W = -2 \log \xi + m(1/\xi)$  where  $m$  is an analytic function of  $1/\xi$ . Then by (3.1)

$$w = \xi^{-2} n(1/\xi)$$

where  $n$  is analytic and  $n(0) \neq 0$ . Then by (4.2)

$$df/d\xi = \xi^{-2} - 5k(1/\xi)$$

where  $k$  is analytic and  $k(0) \neq 0$ . Thus  $f(\xi)$  will be regular at  $\infty$ .

The width of the jet at  $A_1$  in the  $z$ -plane can be determined by considering the expansions

$$\frac{df}{d\xi} = - \frac{2\beta}{U_1 a_3^2 a_5^2 \xi} + \dots$$

$$f = c_1 - \frac{2\beta}{U_1 a_3^2 a_5^2} \log \xi + \dots$$

Then the jump in  $\text{Im} \log \xi$  at  $\xi = 0$  yields for the width at  $A_1$

$$(4.4) \quad h_1 = 2\beta \pi / U_1 a_3^2 a_5^2$$

and rate of mass flow

$$(4.5) \quad M_1 = 2\beta \pi \rho / a_3^2 a_5^2$$

Similarly, at  $A_3$  or  $A_3'$  we have widths

$$(4.6) \quad h_3 = \beta \pi / U_5 a_3^2 (a_5^2 - a_3^2)$$

and rate of mass flow

$$(4.7) \quad M_3 = \beta \pi \rho / a_3^2 (a_5^2 - a_3^2)$$

and at  $A_5$  and  $A_5'$  the total width

$$(4.8) \quad h_5 = 2\beta \pi / U_1 a_5^2 (a_5^2 - a_3^2)$$

and

$$(4.9) \quad M_5 = 2\beta \pi \rho / a_5^2 (a_5^2 - a_3^2)$$

As we would expect from the law of conservation of mass

$$M_1 + M_5 = 2 M_3 .$$

Finally, the ratio of the rate of mass flow at  $A_1$  to that at  $A_5$  is

$$(4.10) \quad M_1/M_5 = a_5^2/a_3^2 - 1$$

In Fig. 1 the straight walls were adjacent to the low pressure regions. Would it be possible to place them adjacent to the high pressure regions? If we proceed purely formally, we merely have to replace the simple poles of  $df/d\xi$  at  $\pm a_3$  by simple poles at  $\pm 1$ . However, the following intuitive considerations show that this process leads at least to an indeterminacy. Suppose a flow of the desired type exists. For our modification consider

$$d \log (df/d\xi)/d\xi = -w'/w + \dots$$

Near the end of one wall the behavior of this logarithmic derivative is dominated by the branch point at  $\xi = a_3$ . But for  $a_3 < \xi < a_4$ ,  $1w'/w < 0$ . Thus, as one would expect, the streamline leaving the wall at  $A_3$  bends initially toward the low pressure region, as shown in Fig. 5. Now, without changing the flow field, we can extend the walls into the stagnant high pressure regions. Since by appropriate changes of scale we can always make the gap between the ends of the extended walls be of unit length, this means that the location of the point of detachment  $A_3$  is indeterminate.

## 5. PARTIALLY CHANNELLED IMPINGING JETS

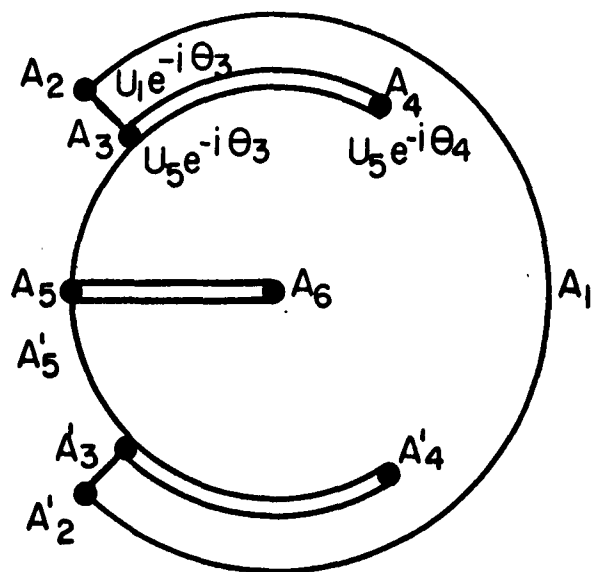
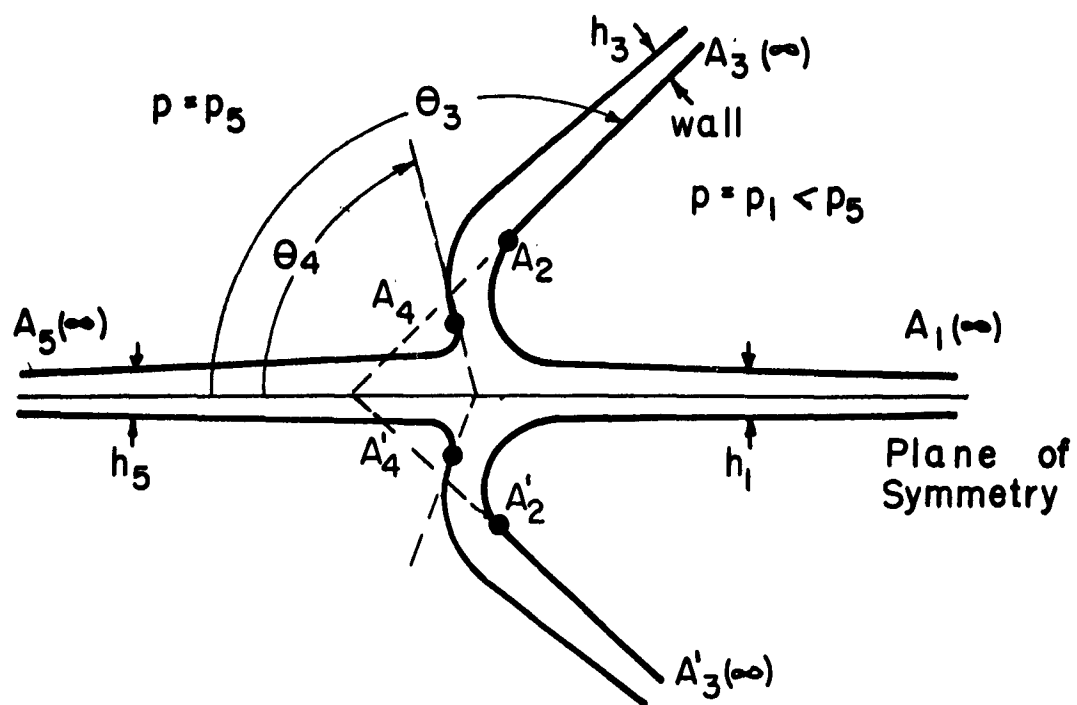
To produce flows with impinging jets that are partially bounded by straight walls on both sides, it will suffice to replace the simple poles of  $df/d\xi$  at  $\pm a_3$  by simple poles at  $\pm a_7$ , where  $1 < a_7 < a_3$ . Now (4.2) becomes

$$(5.1) \quad \frac{df}{d\xi} = -\frac{2\beta}{w} \cdot \frac{1}{\xi (\xi^2 - a_7^2)(\xi^2 - a_5^2)}$$

while (3.2) remains unchanged. The presence of the additional parameter  $a_7$  will make it possible to vary the location of  $A_3$  in Fig. 6, for example, while the locations of  $A_2$  and  $A_4$  and the directions of the walls are held constant.

The calculation of the various jet widths and rates of mass flow are perfectly straightforward exercises which we shall not repeat. It should be remarked that if there is an inflection point  $A_4$  the wall  $A_7A_3$  can be extended into the high pressure region again, just as in the discussion of Fig. 5.

*John H. Giese*  
JOHN H. GIESE



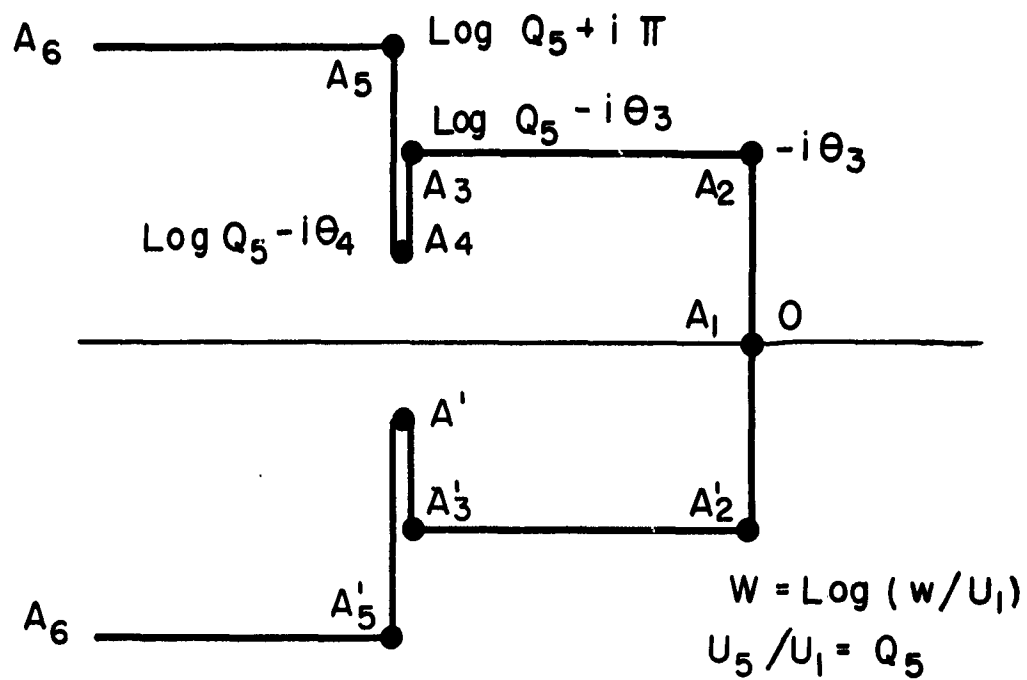


FIG.3 MAP IN  $W$  PLANE

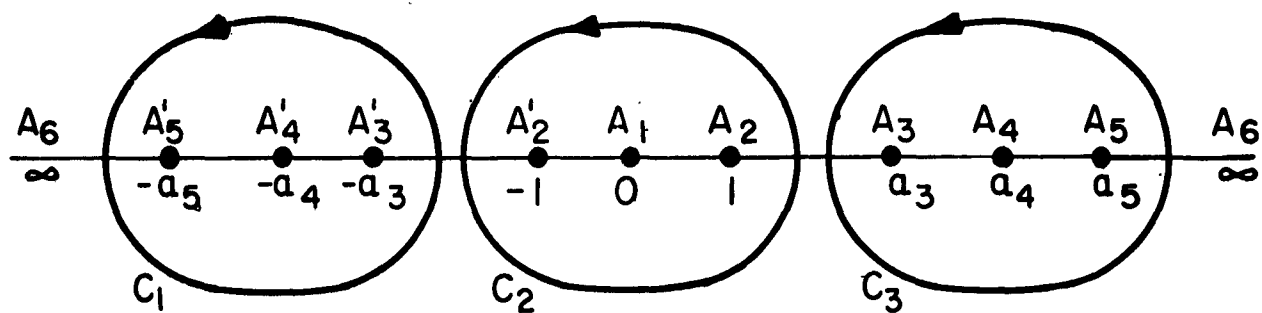
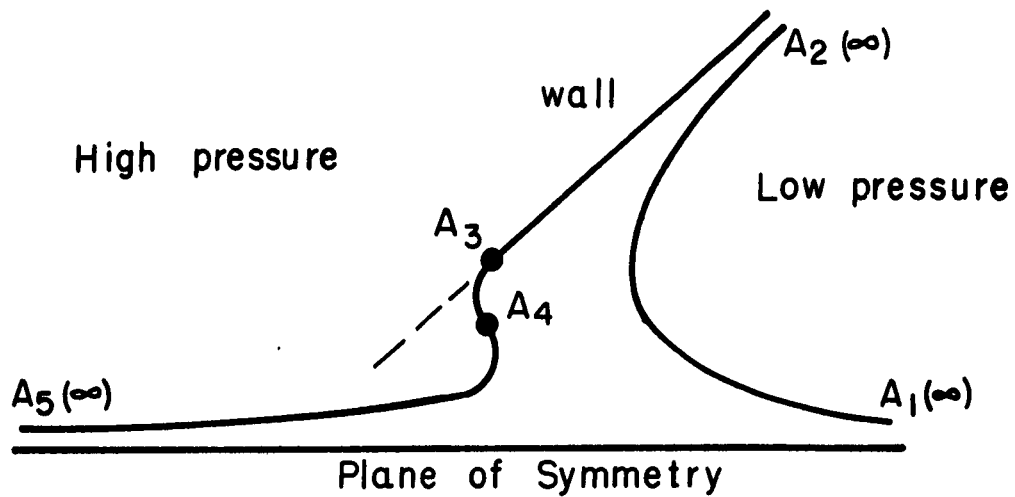
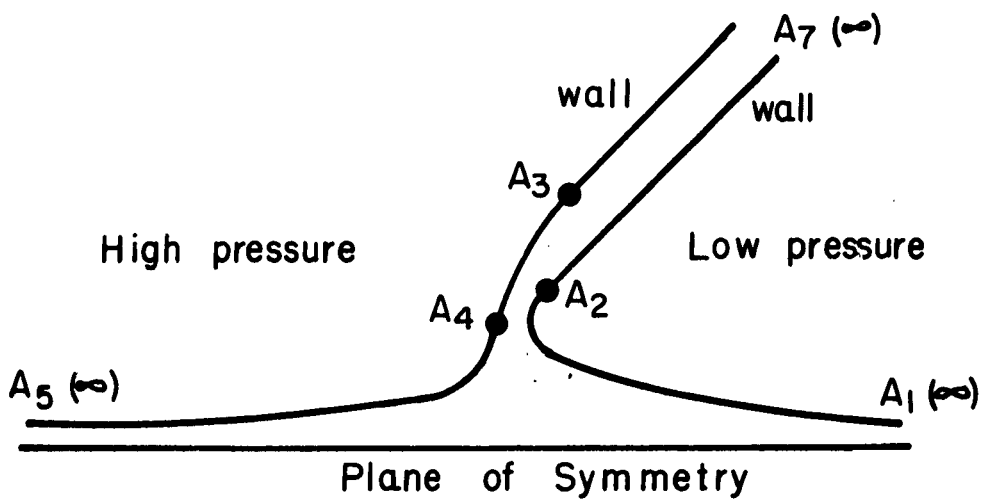


FIG.4 MAP IN  $\zeta$  PLANE



**FIG. 5 INCOMING JET WITH WALL  
ON HIGH PRESSURE SIDE**



**FIG. 6 PARTIALLY CHANNELLED  
INCOMING JET**

# DISTRIBUTION LIST

<u>No. of Copies</u>	<u>Organization</u>	<u>No. of Copies</u>	<u>Organization</u>
10	Commander Armed Services Technical Information Agency ATTN: TIPCR Arlington Hall Station Arlington 12, Virginia	1	Commanding Officer Harry Diamond Laboratories ATTN: Technical Information Office, Branch 012 Washington 25, D. C.
1	Chief Defense Atomic Support Agency Washington 25, D. C.	1	Commanding General Frankford Arsenal ATTN: Library Branch, 0270, Building 40 Philadelphia 37, Pennsylvania
1	Commanding General Field Command Defense Atomic Support Agency Sandia Base P. O. Box 5100 Albuquerque, New Mexico	1	Commanding Officer Rock Island Arsenal Rock Island, Illinois
1	Director of Defense Research and Engineering (OSD) Washington 25, D. C.	1	Commanding Officer Watervliet Arsenal Watervliet, New York
2	Director Advanced Research Projects Agency ATTN: Col. R. Weidler Ballistic Missile Defense Branch Technical Operations Div. Department of Defense Washington 25, D. C.	2	Commanding Officer Picatinny Arsenal ATTN: Feltman Research and Engineering Laboratories Dover, New Jersey
1	Director IDA/Weapon Systems Evaluation Group Room 1E875, The Pentagon Washington 25, D. C.	1	Redstone Scientific Information Center ATTN: Chief, Document Section U. S. Army Missile Command Redstone Arsenal, Alabama
1	Commanding General U. S. Army Materiel Command ATTN: AMCRD-RS-FE-Bal Research and Development Directorate Washington 25, D. C.	2	Commanding Officer Watertown Arsenal Watertown 72, Massachusetts
		1	Commanding General U. S. Army Combat Developments Command ATTN: (CORG) Fort Belvoir, Virginia

# DISTRIBUTION LIST

<u>No. of Copies</u>	<u>Organization</u>	<u>No. of Copies</u>	<u>Organization</u>
1	Commanding Officer U. S. Army Chemical Warfare Laboratories Edgewood Arsenal, Maryland	1	Commandant Army War College Carlisle Barracks, Pennsylvania
1	Commanding General Engineer Research and Development Laboratories U. S. Army Fort Belvoir, Virginia	2	Professor of Ordnance U. S. Military Academy West Point, New York
1	Army Research Office 3045 Columbia Pike Arlington, Virginia	1	Director of Army Research Office, Chief of Research and Development Room 3D-442, The Pentagon Washington 25, D. C.
1	Commanding Officer Army Research Office (Durham) Box CM, Duke Station Durham, North Carolina	1	Chief of Engineers Department of the Army ATTN: ENGNE Mine Warfare Branch Washington 25, D. C.
3	Commanding General Special Weapons Ammunition Command Picatinny Arsenal Dover, New Jersey	4	Chief, Bureau of Naval Weapons ATTN: DIS-33 Department of the Navy Washington 25, D. C.
1	President U. S. Army Artillery Board Fort Sill, Oklahoma	1	Commanding Officer U. S. Naval Air Development Center Johnsville, Pennsylvania
1	President U. S. Army Infantry Board Fort Benning, Georgia	3	Commander U. S. Naval Ordnance Test Station China Lake, California
1	Commandant U. S. Army Artillery and Missile School Fort Sill, Oklahoma	3	Commander U. S. Naval Weapons Laboratory Dahlgren, Virginia
1	Commanding Officer U. S. Army Combat Development Experimentation Center Fort Ord, California	4	Commander Naval Ordnance Laboratory White Oak Silver Spring 19, Maryland

# DISTRIBUTION LIST

<u>No. of Copies</u>	<u>Organization</u>	<u>No. of Copies</u>	<u>Organization</u>
1	Commander U. S. Naval Missile Center Point Mugu, California	2	U. S. Department of Interior Bureau of Mines ATTN: Chief, Explosive and Physical Sciences Div. 4800 Forbes Street Pittsburgh 13, Pennsylvania
3	Director U. S. Naval Research Laboratory Washington 25, D. C.	1	Library of Congress Technical Information Division ATTN: Bibliography Section Reference Department Washington 25, D. C.
1	Commander Operational Test and Evaluation Force U. S. Naval Base Norfolk 11, Virginia	2	Aerojet General Corporation ATTN: Dr. L. Zernow Dr. K. Kreyenhagen 11711 South Woodruff Avenue Downey, California
1	APGC (PGAPI) Eglin Air Force Base, Florida	1	AVCO Corporation Research and Advanced Development Division 201 Lowell Street Wilmington, Massachusetts
1	AFSWC (SWOI) Kirtland Air Force Base New Mexico	2	Explosives Research Group University of Utah Salt Lake City, Utah
1	Director, Project RAND Department of the Air Force 1700 Main Street Santa Monica, California	1	Carnegie Institute of Technology Department of Physics ATTN: Professor Emerson M. Pugh Pittsburgh 13, Pennsylvania
1	Scientific and Technical Information Facility ATTN: NASA Representative (S-AK-DL) P. O. Box 5700 Bethesda, Maryland	1	Firestone Tire and Rubber Company ATTN: Librarian Mr. M. C. Cox Defense Research Division Akron 17, Ohio
1	U. S. Atomic Energy Commission Los Alamos Scientific Laboratory P. O. Box 1663 Los Alamos, New Mexico		
1	U. S. Atomic Energy Commission ATTN: Technical Reports Library Washington 25, D. C.		

# DISTRIBUTION LIST

<u>No. of Copies</u>	<u>Organization</u>	<u>No. of Copies</u>	<u>Organization</u>
3	The General Electric Company Missiles and Space Vehicles Division ATTN: Mr. E. Bruce Mr. R. Soloski Mr. Howard Semon 3198 Chestnut Street Philadelphia 4, Pennsylvania	1	Professor Dr. Ing. Huber Schardin Weil am Rhein, den Rosenstrasse 10 Saint-Louis/Elasas 803 France
2	General Motors Corporation Defense Systems Division Box T Santa Barbara, California	1	Leonard Lundberg Norwegian Defense Research Establishment Lillestrom Norway
1	High Velocity Laboratory University of Utah Salt Lake City, Utah	1	Consulate General of Israel ATTN: Consul in Charge of Scientific Affairs 659 South Highland Avenue Los Angeles 36, California
1	Division of Engineering Brown University Providence, Rhode Island		Of Interest to:  Ministry of Defense Scientific Department Division of Physics P. O. Box 7063 Hakirya
1	Stevens Institute of Technology Davidson Laboratory Castle Point Station Hoboken, New Jersey	1	Commissariat a l' Energie Atomique B. P. No. 7 Sevran (Seine-et-Oise), France
1	Poulter Laboratories Stanford Research Institute Menlo Park, California	1	Dr. S. D. Hamann Commonwealth Scientific and Industrial Research Organization Chemical Research Laboratories Loremer Street Fishermen's Head Victoria, Australia
1	Federal Ministry of Defense Division T II 1 ATTN: Dr. Walter Trinks Bonn-Hardthoehe Germany	3	Mutual Weapons Development Program France Germany Sweden
1	L'Ingenieur Militaire en Chef de 1 Cl Col. De France Ecole Centrale De Pyrotechnie De Bourges, France		

# DISTRIBUTION LIST

<u>No. of Copies</u>	<u>Organization</u>
10	The Scientific Information Officer Defence Research Staff British Embassy 3100 Massachusetts Avenue, N. W. Washington 8, D. C.
4	Defence Research Member Canadian Joint Staff 2450 Massachusetts Avenue, N. W. Washington 8, D. C.

DISTRIBUTION LIST

<u>No. of Copies</u>	<u>Organization</u>
10	The Scientific Information Officer Defence Research Staff British Embassy 3100 Massachusetts Avenue, N. W. Washington 8, D. C.
4	Defence Research Member Canadian Joint Staff 2450 Massachusetts Avenue, N. W. Washington 8, D. C.

<p>AD <u>Accession No.</u>  <u>Ballistic Research Laboratories, AFG</u>  <u>PARTIALLY CONSTRAINED IMPINGING JETS</u>  J. H. Giese</p> <p>ERL Report No. 1202 April 1963</p> <p>ROT &amp; E Project No. 1M010501A003  UNCLASSIFIED Report</p> <p>UNCLASSIFIED</p> <p>Liquid jets -  Impingement  Hydrodynamics -  Jet flow -  Mathematical  Analysis</p> <p>Qualitative explanations of the motion of shaped charge liners have been based on impact of two plane jets in which the moving fluid is surrounded by four stagnant regions, all at the same pressure. Actually, the motion is initiated by the difference between the high pressure in the detonation products on one side of the liner and atmospheric pressure on the other. This report considers symmetrical impact of two jets, each partially constrained on one or both sides, in which the stagnant regions are <u>not</u> all at the same pressure.</p>	<p>AD <u>Accession No.</u>  <u>Ballistic Research Laboratories, AFG</u>  <u>PARTIALLY CONSTRAINED IMPINGING JETS</u>  J. H. Giese</p> <p>ERL Report No. 1202 April 1963</p> <p>ROT &amp; E Project No. 1M010501A003  UNCLASSIFIED Report</p> <p>UNCLASSIFIED</p> <p>Liquid jets -  Impingement  Hydrodynamics -  Jet flow -  Mathematical  Analysis</p> <p>Qualitative explanations of the motion of shaped charge liners have been based on impact of two plane jets in which the moving fluid is surrounded by four stagnant regions, all at the same pressure. Actually, the motion is initiated by the difference between the high pressure in the detonation products on one side of the liner and atmospheric pressure on the other. This report considers symmetrical impact of two jets, each partially constrained on one or both sides, in which the stagnant regions are <u>not</u> all at the same pressure.</p>
<p>AD <u>Accession No.</u>  <u>Ballistic Research Laboratories, AFG</u>  <u>PARTIALLY CONSTRAINED IMPINGING JETS</u>  J. H. Giese</p> <p>ERL Report No. 1202 April 1963</p> <p>ROT &amp; E Project No. 1M010501A003  UNCLASSIFIED Report</p> <p>UNCLASSIFIED</p> <p>Liquid jets -  Impingement  Hydrodynamics -  Jet flow -  Mathematical  Analysis</p> <p>Qualitative explanations of the motion of shaped charge liners have been based on impact of two plane jets in which the moving fluid is surrounded by four stagnant regions, all at the same pressure. Actually, the motion is initiated by the difference between the high pressure in the detonation products on one side of the liner and atmospheric pressure on the other. This report considers symmetrical impact of two jets, each partially constrained on one or both sides, in which the stagnant regions are <u>not</u> all at the same pressure.</p>	<p>AD <u>Accession No.</u>  <u>Ballistic Research Laboratories, AFG</u>  <u>PARTIALLY CONSTRAINED IMPINGING JETS</u>  J. H. Giese</p> <p>ERL Report No. 1202 April 1963</p> <p>ROT &amp; E Project No. 1M010501A003  UNCLASSIFIED Report</p> <p>UNCLASSIFIED</p> <p>Liquid jets -  Impingement  Hydrodynamics -  Jet flow -  Mathematical  Analysis</p> <p>Qualitative explanations of the motion of shaped charge liners have been based on impact of two plane jets in which the moving fluid is surrounded by four stagnant regions, all at the same pressure. Actually, the motion is initiated by the difference between the high pressure in the detonation products on one side of the liner and atmospheric pressure on the other. This report considers symmetrical impact of two jets, each partially constrained on one or both sides, in which the stagnant regions are <u>not</u> all at the same pressure.</p>